An Adaptive Non-linear Statistical Salt-and-Pepper Noise Removal Algorithm using Interquartile Range

Amiya Halder^a, Pritam Bhattacharya^a, and Apurba Sarkar^b

^a St. Thomas College of Engineering and Technology, 4. D. H. Road, Kolkata -700023, India

^b Department of Computer Science and Technology, IIEST Shibpuer, Howrah -711103, India

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Abstract

This paper presents a salt-and-pepper noise removal scheme using modified mean filter. The proposed method is based on a simple basic concepts of mean filter, where each mean value is calculated from the mathematical formula of interquartile range (IQR). It replaces the noisy pixels using IQR based mathematical formula applied on the filter window. Experimental results are presented to demonstrate the efficiency (quality of the image) of the method compared to other existing different types of impulse noise removal techniques.

Key Words: Salt-and-pepper noise, Median filter, IQR, PSNR.

1 Introduction

Salt-and-Pepper noise is a sparsely present white and black pixels as a result of sudden change of maximum (255) and minimum intensity (0) values of pixels. These type of noises generally get introduced in the image during image acquisition phase due to noisy sensor and bit errors in transmission. Salt-and-Pepper noise creates problem in communication for transmission of digital images. These noises needed to be eliminated before the image is fed as input to different image processing applications such as image enhancement, segmentation and recognition etc.

Researchers have been working in this area for decades and various algorithms for removing salt and pepper noise have been proposed. Every algorithm proposed in the literature has its own advantages and disadvantages. It has been observed that, most of the existing noise removal algorithms in the literature are based on linear (such as average filter) and nonlinear (such as standard median filter and modified median filter). Simplest among them is standard median filter (SMF) [1]. It takes a local window of intensities and finds out the median of the intensities which replaces the central pixel of given window in the image. This is highly used due to its simplicity and effectiveness, but this algorithm fails to produce satisfactory results if the noise percentage is more than 40% causing a high blurring effect in the image.

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Correspondence to: <amiya.halder77@gmail.com>

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In the case of weighted median filter (WMF), the standard median filter is modified by assigning the weight value to some of the pixels within a window and in the case of center weighted median filter (CWMF), maximum weight value is set to the central pixel in a window [3, 4]. These weights control the smoothing behavior of the image. WMF, CWMF and other adaptive median filters preserve fine details at the low level of noise density. The tristate median filter (TSMF), which is combination of SMF and CWMF filter is proposed in [5] is able to preserve the fine details but can not work well in case the image has high density of salt-and-pepper noise.

To improve the limitation of median based filters, different types of fuzzy filters and switching median filters have been proposed [10, 11, 13, 12]. In [6], Luo has proposed an efficient technique to remove impulse noise using fuzzy impulse detection(FIDT) technique. The technique presented therein can remove salt-and-pepper noise very efficiently even from a corrupted noise while preserving the image details. Also, in the year 2008, an efficient edge preserving technique has been developed which reduce impulse noise without degrading the image's finer details [9]. These methods work well for images having up to 50% impulse noise density.

To remove the high density of impulse noise and preserve the fine details of image, different kinds of techniques have been proposed, like the noise adaptive fuzzy switching median filter (AFSMF) [15], modified decision based unsymmetric trimmed median filter (UTMF) [16], the the fast and efficient median filter (FEMF) [14], sorted switching median filter [17], decision-based coupled window median filter [18], improvement of Decision median filter for suppression of salt-and-pepper noise (IDMF)[2], new decision-based trimmed median filter (DTMF) [19] and an efficient restoration algorithm [ERA] [20] etc.

In this paper, we present a new type of modified mean filter for detecting and removing impulse noise using mathematical concept of median and interquartile range (IQR). The proposed filtering technique is simple and adaptive. The adaptive nature allows the filter to increase the size of its window according to local noise density.

Rest of the paper is organized as follows. The proposed method is introduced in Sec. 2. Section 3 presents simulation results obtained by the proposed method with brief analysis and provides comparison with existing techniques. Finally, in Sec. 4 the paper is concluded.

2 Proposed Method

The proposed filter is designed by modifying the existing adaptive modified mean filter with mathematical concepts of the Nonparametric Univariate Statistics for Quantitative Variables: the median and the interquartile range (IQR). To explain, let us consider $\xi(P,Q)$ be an image with the number of rows as P and number of columns as Q. The method processes the noisy images by detecting the salt-and-pepper noise. Salt noises are the pixels with intensity value 0 and pepper noises are the pixels with intensity value 0 and pepper noises are the pixels with intensity values 255. If the intensity of the pixel being processed lies between 0 and 255 then it is a noise free pixel and it is left unchanged. On the other hand if the intensity value of the pixel is equal to 0 or 255, then it is a noisy pixel and is processed by proposed filter as follows. If a noisy pixel is found then a square filtering window $H_{(2w+1)(2w+1)}(\mu,\nu) = \{h(\mu + m, \nu + n)\}$, where $h(\mu, \nu)$ is pixel intensity of point (μ, ν) and $m, n \in (-w,0,w)$ is considered. From this window, non-noisy pixels are found out. If all the pixels are noisy, then the window size is increased. Let $N_{\mu,\nu}$ is defined as the set of all non-noisy pixels in the neighborhood of the point $h(\mu, \nu)$.

$$N_{\mu,\nu} = \{h(k,l) \neq (0,255) : k = [\mu - m, \mu + m], l = [\nu - n, \nu + n]\}$$
(1)

Let the members of the set $N_{\mu,\nu}$ are $Z_{p+1}, Z_{p+2}, Z_{p+3}, ..., Z_{p+q}$ where q is the number of elements in $N_{\mu,\nu}$. These noise free pixels are arranged in the sorted order of intensity value i.e., $Z_{p+1} <= Z_{p+2} <= <= Z_{p+q}$. Then the index of the minimum value (χ_l) and the maximum value (χ_u) in sorted list are selected. The interquartile range (IQR) is the range of values within which reside in the middle 50% of the elements with the middle element at $\frac{(\chi_l + \chi_u)}{2}$. Now, if we consider total number elements which is $(\chi_u - \chi_l + 1)$, then range of the IQR is from index $\frac{(\chi_l + \chi_u)}{4}$ to index $\frac{3*(\chi_l + \chi_u)}{4}$. The lower bound of the interquartile range is called the first quartile (P_1) of the list and contains all the elements in the index range from χ_l to $\frac{(\chi_l + \chi_u)}{4}$. The upper bound of the interquartile range is called the third quartile (P₃) of the list and contains all the elements in the index ranges from $\frac{3*(\chi_l+\chi_u)}{4}$ to $(\chi_u - \chi_l + 1)$.

The proposed method is based on the above concepts. In the case of average filter, the center pixel is replaced by the average value of the $(2w + 1) \times (2w + 1)$ window. But, in the proposed method following formula is used.

$$S_{\mu,\nu} = \frac{\sum_{q=\frac{(\chi_l+\chi_u)}{4}}^{\frac{3*(\chi_l+\chi_u)}{4}} Z_q}{\frac{3*(\chi_l+\chi_u)}{4} - \frac{(\chi_l+\chi_u)}{4} + 1}$$
(2)

In the case of median filter all non noisy pixels in the $(2w + 1) \times (2w + 1)$ window are sorted in the ascending order of their intensity value, and the median of the sorted values are found out. Subsequently, the noisy pixels are replaced with this median. But in that case the precision of the noise removal is very poor. It is observed that, the values within the range $\frac{(\chi_l + \chi_u)}{4}$ to $\frac{3*(\chi_l + \chi_u)}{4}$ are near to median and far to 0 and 255. So, in the proposed method, the noisy pixels are replaced with the mean of the range from $\frac{(\chi_l + \chi_u)}{4}$ to $\frac{3*(\chi_l + \chi_u)}{4}$ producing a better precision. It is to be noted here that we are not considering the range χ_l to $\frac{(\chi_l + \chi_u)}{4}$ because they will be blackish in nature and also not considering the range $\frac{3*(\chi_l + \chi_u)}{4}$ to $(\chi_u - \chi_l + 1)$ because they will be whitish in nature.

2.1 Explanation of the proposed method

The working principle of the proposed method is described using a 3×3 selected window as follows:

0	20	40
50	255	0
132	0	90

Let us consider the noisy pixel is at the center of the selected window 255 (processing pixel) and neighbours of this pixels are $N = \{20, 40, 50, 132, 90\}$ (noise free pixels). Now, these values are sorted in ascending order $N = \{20, 40, 50, 90, 132\}$ and the total number of pixel is n = 5, the lower index is $\chi_l = 0$, upper index is $\chi_u = 4$ and median of the indices is $\frac{(\chi_l + \chi_u)}{2} = 2$. So, IQR is calculated from 1(n/4 = 5/4 = 1) to 3(3n/4 = 3 * 5/4 = 3), and its value is

$$S_{\mu,\nu} = \frac{\sum_{q=\frac{5}{4}}^{\frac{3+5}{4}} Z_q}{\frac{3+5}{4} - \frac{5}{4} + 1} = \frac{\sum_{q=1}^{3} Z_q}{3 - 1 + 1} = \frac{\sum_{q=1}^{3} Z_q}{3} = \frac{Z_1 + Z_2 + Z_3}{3} = \frac{40 + 50 + 90}{3} = 60$$
(3)

Finally, the noisy pixel 255 (center of the window) is replaced by the value of 60 (i.e. $S_{\mu,\nu}$). After removing the noisy pixel, the modified selected window is shown below:

0	20	40
50	60	0
132	0	90

In case the center pixel in the selected 3×3 window is noisy (0 or 255) and all neighborhood pixels of window are also noisy, then the window size is increased to $5 \times 5, 7 \times 7, \ldots$ and so on. The process is explained again with a window size of 5×5 .

The center is 0 of the 3×3 selected window and all the neighbors are also noisy pixels, so increased the window size 5×5 . In 5×5 window, the noise free pixels are $N = \{60, 20, 40, 30, 50, 45, 70, 80, 55\}$. Now, these values are sorted in ascending order $N = \{20, 30, 40, 45, 50, 55, 60, 70, 80\}$ and the total number of pixel

60	20	40	30	255
50	0	0	255	45
70	0	\bigcirc	0	255
80	0	0	0	255
255	55	0	0	0

is n = 9, the lower index is $\chi_l = 0$, upper index is $\chi_u = 8$ and median of the indices is $\frac{(\chi_l + \chi_u)}{2} = 4$. So, IQR is calculated from 2(n/4 = 9/4 = 2) to 6(3n/4 = 3 * 9/4 = 6), and its value is

$$S_{\mu,\nu} = \frac{\sum_{q=\frac{9}{4}}^{\frac{3*9}{4}} Z_q}{\frac{3*9}{4} - \frac{9}{4} + 1} = \frac{\sum_{q=2}^{6} Z_q}{6 - 2 + 1} = \frac{\sum_{q=2}^{6} Z_q}{5} = \frac{Z_2 + Z_3 + Z_4 + Z_5 + Z_6}{5} = \frac{40 + 45 + 50 + 55 + 60}{5} = 50$$
(4)

The noisy pixel 0 (center of the window) is replaced by the value of 50 (i.e. $S_{\mu,\nu}$). After removing the noisy pixel, the processing window is shown below:

60	20	40	30	255
50	0	0	255	45
70	0	(50)	0	255
80	0	0	0	255
255	55	0	0	0

3 Results and analysis

The performance of the proposed method is compared with a number of existing filtering techniques. To evaluate the performance, several quantitative measures(criteria) are calculated. The quantitative measures include root-mean square error (RMSE), peak signal to noise ratio (PSNR), image enhancement factor (IEF), and structural similarity (SSIM), which are given in Eqs. 5, 6, 7, 8 respectively.

$$PSNR(\xi_1, \xi_2) = 20 \log_{10} \frac{255}{RMSE}$$
(5)

$$RMSE(\xi_1,\xi_2) = \sqrt{\left(\frac{1}{P \times Q} \sum_{p=1}^{P} \sum_{q=1}^{Q} |\xi_1(p,q) - \xi_2(p,q)|^2\right)}$$
(6)

$$IEF(\xi_1, \xi_2, \xi_3) = \frac{\sum_{p=1}^{P} \sum_{q=1}^{Q} [\xi_1(p, q) - \xi_3(p, q)]^2}{\sum_{p=1}^{P} \sum_{q=1}^{Q} [\xi_1(p, q) - \xi_2(p, q)]^2}$$
(7)

$$SSIM = \frac{(2\omega_{\xi_1}\omega_{\xi_2} + k_1) + (2\nu_{\xi_1\xi_2} + k_2)}{(\omega_{\xi_1}^2 + \omega_{\xi_2}^2 + k_1) + (\nu_{\xi_1}^2 + \nu_{\xi_2}^2 + k_2)}$$
(8)

where $\xi_1(p,q), \xi_2(p,q), \xi_3(p,q)$ are pixels of the original image ξ_1 , restored image ξ_2 and corrupted image ξ_3 of size $P \times Q$ respectively. $\omega_{\xi_1}, \omega_{\xi_2}$ are the average intensities and ν_{ξ_1}, ν_{ξ_2} are standard deviations of image ξ_1, ξ_2 respectively. $\nu_{\xi_1\xi_2}$ is the covariance of the two images. k_1 and k_2 are constants value and are set to $(0.01 \times 255)^2$ and $(0.03 \times 255)^2$.

The estimation of salt and pepper noise suppression is performed using 8-bit gray scale images, Airplane, Lena, Bridge, Boats, Mandrill, Peppers, Zelda, Barbara, Goldhill, Flower, Lighthouse, Girl, Moon, and Parrots with different resolutions 512×512 , 256×256 , 787×576 , 720×576 , 512×768 . The proposed method is compared with classic filters such as SMF [1] and other recent state-of-the-art techniques like FIDT [6], AFSMF [15], UTMF [16], IDMF [2], DTMF [19] and ERA [20].

Table. 1, Table. 2, Table. 3, and Table. 4 show the restoration results based on comparisons of PSNR(dB), RMSE and IEF and SSIM values obtained by the above existing method and the proposed algorithm for an Airplane image corrupted with the noise density 10%, 20%, 30%, 40%, 50%, 60%, 70%, 80%, 90%, and 99%. From these table, upto 50% of noise density all method gives good results to remove impulse noise and preserve more details. This proposed method can successfully remove the noise even at high density noise ratios, and preserve fine edges in the process of denoising.

Table 1: RMSE value of the various noise density 10% to 99% using SMF, FIDT, UTMF, AFSMF, IDMF, DTMF ERA and Proposed method for Airplane image.

Noise density (%)	10%	20%	30%	40%	50%	60%	70%	80%	90%	95%	99%
										123.11	
											137.26
UTMF	2.91	4.46	6.56	8.28	10.84	14.20	19.40	30.91	56.57	75.49	97.41
										46.77	
										55.52	
DTMF	2.97	4.59	6.00	7.27	8.64	10.18	12.12	14.74	20.91	28.16	44.48
										20.94	
Proposed method	2.62	3.91	5.04	6.13	7.19	8.51	10.26	12.27	16.23	20.63	32.92

Table 2: PSNR value of the various noise density 10% to 99% using SMF, FIDT, UTMF, AFSMF, IDMF, DTMF ERA and Proposed method for Airplane image.

Noise density (%)	10%	20%	30%	40%	50%	60%	70%	80%	90%	95%	99%
	30.82										
FIDT	38.64	34.92	31.19	28.19	24.28	20.89	17.04	13.56	9.51	7.35	5.37
UTMF	38.82	35.13	31.79	29.76	27.42	25.08	22.37	18.32	13.07	10.57	8.35
AFSMF	38.44	34.82	32.28	30.40	28.56	26.55	24.25	22.27	19.19	14.77	7.93
IDMF	31.60	30.80	29.33	28.19	26.65	25.26	22.35	19.21	15.20	13.24	10.30
DTMF	38.66	34.88	32.55	30.89	29.39	27.96	26.45	24.75	21.72	19.13	15.16
	30.05										
Proposed method	39.76	36.27	34.07	32.37	30.98	29.52	27.90	26.35	23.92	21.83	17.77

Table 3: IEF value of the various noise density 10% to 99% using SMF, FIDF, UTMF, AFSMF, IDMF, DTMF ERA and Proposed method for Airplane image.

Noise density (%)	10%	20%	30%	40%	50%	60%	70%	80%	90%	95%	99%
SMF	39.2227	52.0220	45.0219	39.0067	25.9592	15.9179	8.0366	4.1279	1.9082	1.3236	1.0544
FIDT	237.5110	201.6395	128.0174	85.4223	43.4505	23.9387	11.5200	5.9024	2.6188	1.6798	1.1069
UTMF	247.6817	211.3212	146.9016	122.6140	89.5723	62.7516	39.2956	17.6739	5.9487	3.5200	2.1977
AFSMF	226.8228	197.0394	164.7058	142.1571	116.4226	88.0235	60.6538	43.8631	43.8631	24.3337	9.2746
IDMF	46.9830	78.0337	83.4129	85.4539	75.0333	65.3979	39.1682	21.6632	9.7029	6.5072	3.4398
DTMF	238.7518	199.4038	175.1922	159.0205	141.0029	122.0603	100.6407	77.6854	43.5323	25.2845	10.5402
ERA	32.8190	57.1811	57.4877	73.7596	87.2828	93.0120	82.9751	79.2974	60.2852	45.7326	5.5384
Proposed method	307.1414	275.2047	248.6116	223.9391	203.4162	174.5540	140.3543	112.1143	72.2631	47.0942	19.2346

Figure. 1-4 show the denoised image of Airplane using the methods SMF, FIDT, AFSMF, UTMF, IDMF, DTMF, ERA and the proposed method with a noise ratio of 20%, 40%, 70% and 90%. Also, Figure. 5-8 show the output denoised image of Boat image using the above methods. From the above results, SMF gives poor performance in all noise densities. FIDT, UTMF, and IDMF filters have considerable improvements over SMF. AFSMF, DTMF and ERA performs better than the FIDT, UTMF, and IDMF filters with respect

Table 4: SSIM value of the various noise density 10% to 99% using SMF, FIDT, UTMF, AFSMF, IDMF, DTMF ERA and Proposed method for Airplane image.

Noise density (%)		20%	30%	40%	50%	60%	70%	80%	90%	95%	99%
SMF	0.9926	0.9899	0.9854	0.9782	0.9632	0.9336	0.8593	0.7346	0.4973	0.3675	0.2854
FIDT	0.9990	0.9977	0.9950	0.9902	0.9791	0.9555	0.9005	0.8057	0.5892	0.4445	0.2992
UTMF	0.9990	0.9978	0.9957	0.9930	0.9889	0.9816	0.9689	0.9395	0.8002	0.6380	0.4353
		0.9980									
		0.9944									
DTMF	0.9991	0.9980	0.9960	0.9944	0.9920	0.9890	0.9834	0.9762	0.9572	0.9290	0.8317
		0.9866									
Proposed method	0.9991	0.9981	0.9969	0.9956	0.9937	0.9913	0.9878	0.9828	0.9710	0.9577	0.8589

quality measurement parameters such as RMSE, PSNR, IEF, and SSIM. Compared to such existing filters, the proposed method has significant improvement. Figure. 9 shows the local features (RMSE, PSNR, IEF and SSIM) for Boat image using existing filters; SMF, FIDT, AFSMF, UTMF, IDMF, DTMF, ERA and proposed method with noise density 10% to 90%.

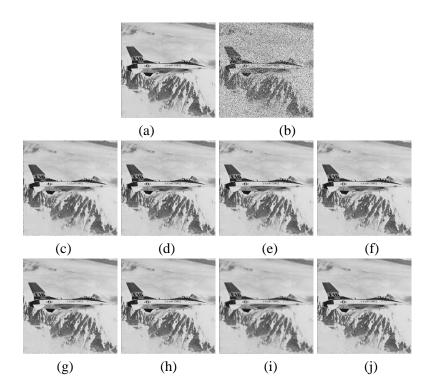


Figure 1: Output results for Airplane image corrupted with 30% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

Figure. 10 - 11 show the denoised image for Goldhill image with corrupted 20%, 40% noise ratio of all the above methods, respectively. Compared with all the results, theoretically and visually our proposed method gives the better results than the above existing noise removal algorithms.

Figure. 12 - 13 show the denoised image for Lena, Mandrill, Goldhill and Zelda images with 80% and 90% noise ratio using SMF, FIDT, AFSMF, UTMF, IDMF, DTMF, ERA and proposed method. Figure. 14 shows the local features average PSNR and average SSIM of traditional 12 images. From experimental results, our proposed method gives the improvement results than the above existing noise removal techniques.

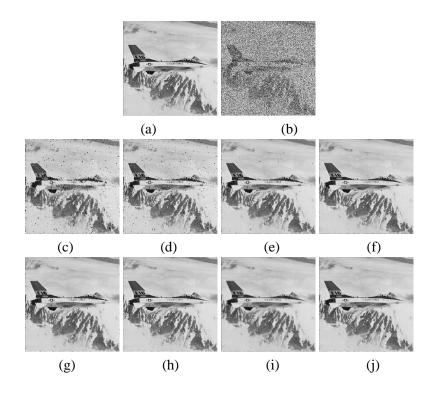


Figure 2: Output results for Airplane image corrupted with 60% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

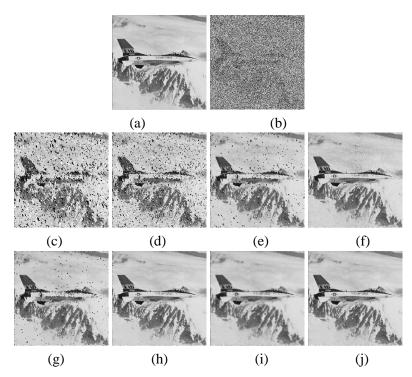


Figure 3: Output results for Airplane image corrupted with 80% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

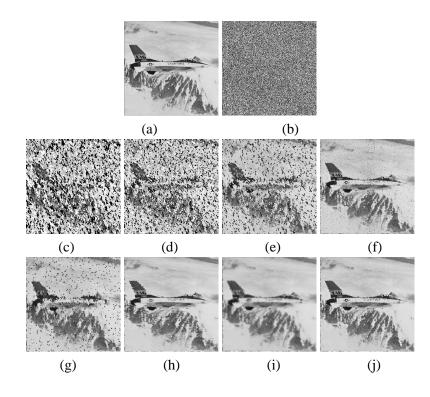


Figure 4: Output results for Airplane image corrupted with 90% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

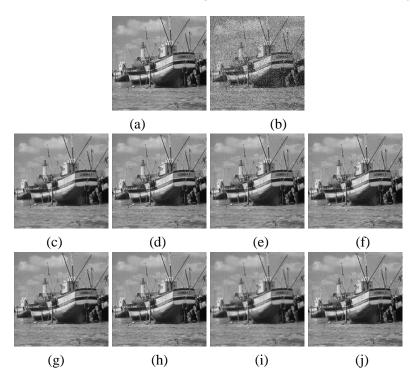


Figure 5: Output results for Boat image corrupted with 20% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d)FIDT, (e)UTMF, (f) AFSMF, (g) IDMF, (h)DTMF, (i) ERA and (j) Proposed method.

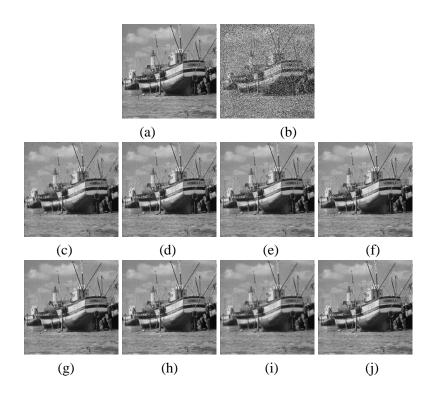


Figure 6: Output results for Boat image corrupted with 40% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

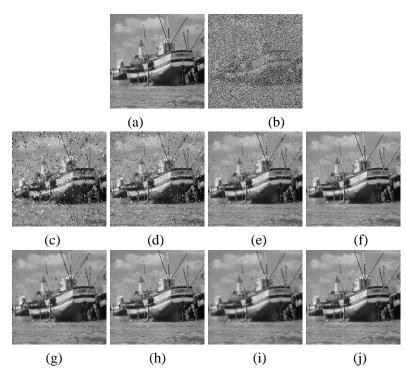


Figure 7: Output results for Boat image corrupted with 70% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

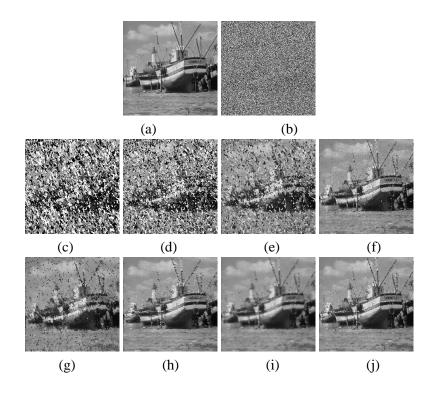


Figure 8: Output results for Boat image corrupted with 90% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

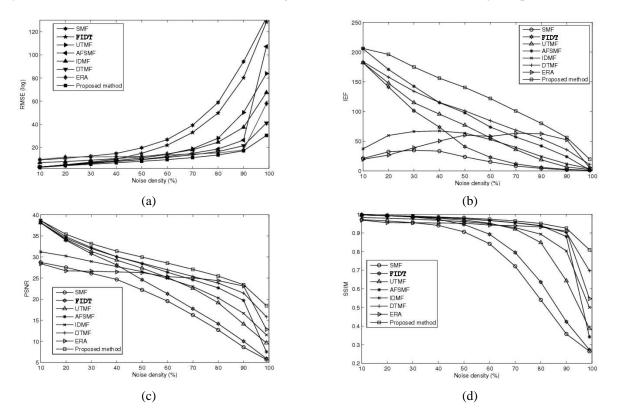


Figure 9: Comparison of Boat images: (a) RMSE (b) IEF (c) PSNR and (d) SSIM.

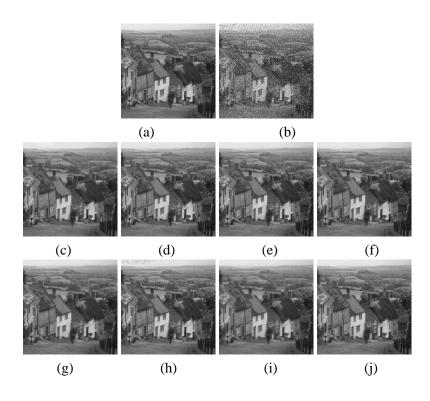


Figure 10: Output results for Goldhill image corrupted with 20% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

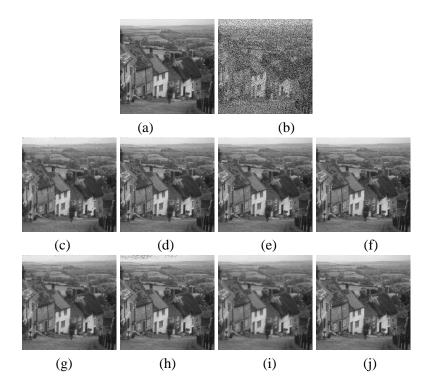


Figure 11: Output results for Goldhill image corrupted with 40% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.



Figure 12: Output results for goldhill image corrupted with 80% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA (j) Proposed method.

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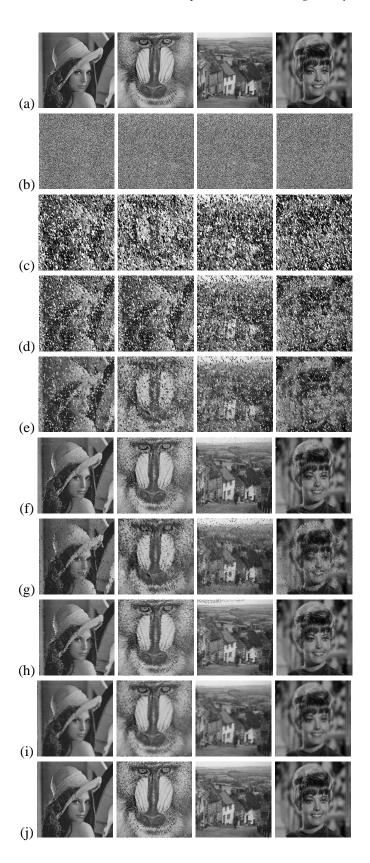


Figure 13: Output results for Goldhill image corrupted with 90% salt-and-pepper noise density. (a) Original, (b) noisy, (c) SMF, (d) FIDT, (e) UTMF, (f) AFSMF, (g) IDMF, (h) DTMF, (i) ERA and (j) Proposed method.

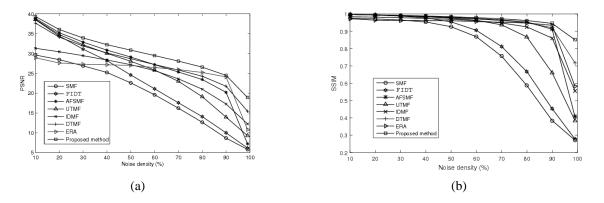


Figure 14: Comparison of the average (a) PSNR and (b) SSIM value of the twelve Traditional images.

4 Conclusion

This paper presents a simple technique to remove salt-and-pepper noise present in different type of images. The technique is based on the mathematical formula of Interquartile range. The proposed technique successfully removes every noisy pixel with suitable intensity value which is calculated based on steps outlined earlier. It has been observed from the experimental results that the proposed method performs better than existing techniques as well as preserve the fine details of the images even if the original image contains high density salt-and-pepper noise. The subjective, as well as objective experimental testing, suggests that the proposed algorithm provides enhanced performance for removing the salt-and-pepper noise overall noise density levels. The proposed technique can be used as pre-processing steps to remove noise in many real-life applications such as medical images and noisy satellite images. With little modification, it can also be applicable to noisy color images.

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